

Unclassified

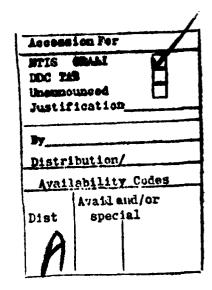
SECURITY CLASS FIGATION OF THIS PAGE (When Date Entered)	
REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM
, · · · · · · · · · · · · · · · · · · ·	3. PECIPIFNT'S CATALOG HUMBER
RADC-TR-79-358/ \( \text{AD-A085 568}	
TITLE (and Babillia)	S. TYPE OF REPORT & PERIOD COVERE
ANTENNA, TECHNOLOGY FOR SPACE BASED	In House
BADAR, PART I. SUBARRAYING FEEDS: BANDWIDTH, LOW SIDELOBE PERFORMANCE AND SUBARRAY NULLING	
BANDWIDTH, LOW, SIDELOBE PERFORMANCE	6. PERFORMING ORG. REPORT NUMBER
AND SUBARRAY NULLING	S. CONTRACT OR GRANT NUMBER(a)
The same of the sa	
Robert J. Mailloux	
And the second s	
Deputy for Electronic Technology (RADC/EEA)	10. PROGRAM ELEMENT, PROJECT, TASK APEA A WORK WHIT MUMBERS.
Hanscom AFB	62702F (17)IL/ (
Massachusetts 01731	4690 401
11. CONTROLLING OFFICE NAME AND ADDRESS	12. REPORT DATE
Deputy for Electronic Technology (RADC/EEA)//	February 1089
Hanscom AFB	18-HUNDER TIP PROCE
Massachusetts 01731	17
14. MONITORING AGENCY HAME & ADDRESSELL different from Controlling Office)	15. SECURITY CLASS. (of this report)
12:19	Unclassified
-1	15a. DECLASSIFICATION/DOWNGRADING
,	SCHEDULE
Approved for public release; distribution unlimited	nTIC
Approved for public release; distribution unlimited	DTIC
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abelraci entered in Block 29, if different free	DTIC
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abelraci entered in Block 29, if different free	DTIC
Approved for public release; distribution unlimited	DTIC
16. DISTRIBUTION STATEMENT (of this Report)  Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abotract entered in Block 26, if different free  18. SUPPLEMENTARY NOTES  19. KEY WORDS (Continue on reverse side if necessary and identify by block number)	JUN 1 6 M
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abetract entered in Block 26, 16 different from  18. SUPPLEMENTARY NOTES  19. REV WORDS (Continue on reverse side if necessary and identify by block number)  Antenna	JUN 1 6 M
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abotract entered in Block 26, if different free  18. SUPPLEMENTARY NOTES  19. KEY WORDS (Continue on reverse olds if necessary and identify by block number)  Antenna  Phased array	JUN 1 6 M
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different free  18. SUPPLEMENTARY NOTES  19. KEY WORDS (Continue on reverse olds if necessary and identify by block number) Antenna Phased array Subarrays	JUN 1 6 Y
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different free  18. SUPPLEMENTARY NOTES  19. KEY WORDS (Continue on reverse olds if necessary and identify by block number)  Antenna  Phased array  Subarrays	JUN 1 6 Y
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the about act entered in Block 20, if different free  18. SUPPLEMENTARY NOTES  19. REV WORDS (Continue on reverse side if necessary and identify by block number) Antenna Phased array Subarrays Low sidelobe arrays	JUN 1 6 M
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the obstract entered in Block 26, if different free  18. SUPPLEMENTARY NOTES  19. KEY WORDS (Continue on reverse olds if necessary and identify by block number)  Antenna  Phased array  Subarrays  Low sidelobe arrays  20. ABSTRACT (Continue on reverse olds if necessary and identify by block number)  This brief analysis outlines the features of a s	JUN 1 6 M
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abotract entered in Block 20, if different free  18. SUPPLEMENTARY HOTES  19. KEY WORDS (Continue on reverse side if necessary and identify by block number)  Antenna  Phased array  Subarrays  Low sidelobe arrays  M. ABSTRACT (Continue on reverse side if necessary and identify by block number)  This brief analysis outlines the features of a samplitude control circuits at the feed array face.	JUN 1 6 Y  ubarraying system with The analysis treats the
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abotract entered in Block 26, if different feet  18. SUPPLEMENTARY NOTES  19. KEY WORDS (Continue on reverse olds if necessary and identify by block number)  Antenna  Phased array  Subarrays  Low sidelobe arrays  M. ABSTRACT (Continue on reverse olds if necessary and identify by block number)  This brief analysis outlines the features of a samplitude control circuits at the feed array face, idealization of the lens feed as a continuous aperture.	ubarraying system with The analysis treats the re, and includes the
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abotract entered in Block 26, if different feet  18. SUPPLEMENTARY NOTES  19. KEY WORDS (Continue on reverse olds if necessary and identify by block number)  Antenna  Phased array  Subarrays  Low sidelobe arrays  Apstract (Continue on reverse olds if necessary and identify by block number)  This brief analysis outlines the features of as amplitude control circuits at the feed array face, idealization of the lens feed as a continuous aperture assumption that the cylindrical lens back face is in	ubarraying system with The analysis treats the re, and includes the the far field of the array
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the about act entered in Block 26, if different free  18. SUPPLEMENTARY NOTES  19. REV WORDS (Continue on reverse side if necessary and identify by block number) Antenna Phased array Subarrays Low sidelobe arrays  10. Approact (Continue on reverse side if necessary and identify by block number) This brief analysis outlines the features of a samplitude control circuits at the feed array face, idealization of the lens feed as a continuous aperture assumption that the cylindrical lens back face is in feed. The analysis includes the effect of truncation	ubarraying system with The analysis treats the re, and includes the the far field of the array at the main array, and
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the about act entered in Block 20, if different free  18. SUPPLEMENTARY NOTES  19. HEV WORDS (Continue on reverse side if necessary and identify by block number) Antenna Phased array Subarrays Low sidelobe arrays  18. ABSTRACT (Continue on reverse side if necessary and identify by block number) This brief analysis outlines the features of a samplitude control circuits at the feed array face, idealization of the lens feed as a continuous aperture assumption that the cylindrical lens back face is in feed. The analysis includes the effect of truncation demonstrates that the high sidelobes of the convent	ubarraying system with The analysis treats the re, and includes the the far field of the array at the main array, and ional sin x/x subarray
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the about act entered in Block 20, if different free  18. SUPPLEMENTARY NOTES  19. REV WORDS (Continue on reverse side if necessary and identify by block number) Antenna Phased array Subarrays Low sidelobe arrays  20. ADSTRACT (Continue on reverse side if necessary and identify by block number) This brief analysis outlines the features of a samplitude control circuits at the feed array face, idealization of the lens feed as a continuous aperture assumption that the cylindrical lens back face is in feed. The analysis includes the effect of truncation demonstrates that the high sidelobes of the convent illumination, when truncated, are primary contributions.	ubarraying system with The analysis treats the re, and includes the the far field of the array at the main array, and ional sin x/x subarray utors to high grating lobe
Approved for public release; distribution unlimited  17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different free  18. SUPPLEMENTARY NOTES  19. HEV WORDS (Continue on reverse side if necessary and identify by block number) Antenna Phased array Subarrays Low sidelobe arrays  M. ADSTRACT (Continue on reverse side if necessary and identify by block number)  This brief analysis outlines the features of a samplitude control circuits at the feed array face, idealization of the lens feed as a continuous aperture assumption that the cylindrical lens back face is in feed. The analysis includes the effect of truncation demonstrates that the high sidelobes of the convent illumination, when truncated, are primary contribulevels under certain circumstances. The proposed	ubarraying system with The analysis treats the re, and includes the the far field of the array at the main array, and ional sin x/x subarray utors to high grating lobe
Approved for public release; distribution unlimited  7. DISTRIBUTION STATEMENT (of the abetract entered in Block 20, if different free  8. SUPPLEMENTARY NOTES  8. SUPPLEMENTARY NOTES  9. KEY WORDS (Continue on reverse side if necessary and identify by block number)  Antenna  Phased array  Subarrays  Low sidelobe arrays  1. ABSTRACT (Continue on reverse side if necessary and identify by block number)  This brief analysis outlines the features of a samplitude control circuits at the feed array face, idealization of the lens feed as a continuous aperture assumption that the cylindrical lens back face is in feed. The analysis includes the effect of truncation fermonstrates that the high sidelobes of the convent illumination, when truncated, are primary contributed and the certain circumstances. The proposed promes is a substract.	ubarraying system with The analysis treats the re, and includes the the far field of the array at the main array, and ional sin x/x subarray utors to high grating lobe

319000

ジ

truncation effects is to produce a low sidelobe subarray illumination at the main aperture by controlling the feed array taper. Numerical results show the effectiveness of this subarraying technique for controlling the array far sidelobes and grating lobe levels, and for producing wide band null troughs within the subarray pattern.

Unclassified



## **Contents**

1.	INTRODUCTION	5
2.	RADIATION CHARACTERISTICS OF THE SYSTEM	5
3.	CONCLUSION	17

# Illustrations

1.	Subarraying Feed for Phase Scanned Lens	6
2.	Subarray Feed With no Output Taper:  A. Edge Subarray Pattern (p = -3)  B. Central Subarray Pattern (p = -1)  C. Radiation Pattern for Uniformally Illuminated Array  D. Radiation Pattern for Array With -35 dB-Chebyshev Taper	9
3.	Subarray Feed With Tapered Output:  A. Edge Subarray Pattern (p = -3)  B. Central Subarray Pattern (p = -1)  C. Radiation Pattern for Uniformally Illuminated Array  D. Radiation Pattern for Array With -35 dB Chebyshev Taper	10
4.	Subarray Pattern for the Truncated Distribution of Eq. (12)	11
5.	Subarray Patterns for the Illumination of Eq. (14)	12
6A	. Narrowed Subarray for Interference Rejection	16
6B	Narrowed Subarray Pattern Using Eq. (8)	16

## Antenna Technology for Space Based Radar Part I. Subarraying Feeds: Bandwidth, Low Sidelobe Performance and Subarray Nulling

#### 1. INTRODUCTION

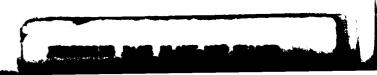
Future space-based and ground radar systems will require wideband scanning arrays with sidelobes below -40 dB, steered nulls, and other forms of active pattern control. Since the cost of a fully time-delay steered array is prohibitive for many of these applications, there is a need for subarraying feeds so that time-delay and/or null steering can be controlled at the relatively fewer subarray inputs, while the main aperture need only have conventional phase shifters. Tang¹ described a number of subarraying feeds with varying degrees of "overlap" and using constrained or space-fed geometries. The feed system referred to by Tang as "completely overlapped" is investigated in this paper to determine its suitability for forming very low sidelobe scanned patterns and for producing nulls in the subarray pattern.

### 2. RADIATION CHARACTERISTICS OF THE SYSTEM

Figure 1 shows the basic configuration using a one-dimensional circular lens and fixed time delays at the hybrid matrix output for subarray collimation. This

(Received for publication 7 February 1980)

 Tang, R. (1972) Survey of time delay beam steering techniques in phased array antennas, in <u>Proceedings of the 1970 Phased Array Antenna Symposium</u>, Artech House, Inc., Dedham, MA, pp 254-260.



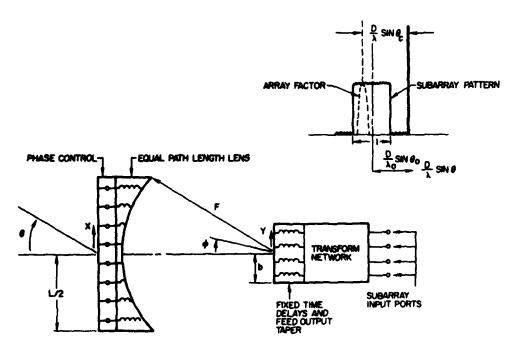


Figure 1. Subarraying Feed for Phase Scanned Lens

specific implementation was proposed by Borgiotti<sup>2</sup> for a similar subarraying system that scanned over a limited spatial sector. The main array has phase shifters to produce a phase tilt that scans the subarray patterns. The feed is a Fourier transformer in the form of a hybrid matrix or multiple beam lens, but for the purposes of this analysis a multiple beam lens with true time delay will be assumed. In addition, the feed array and the lens! faces will be modeled as continuous apertures, and the projection factor  $\cos \theta$  will be suppressed for convenience.

The purpose of the multiple beam feed is to form a group of N-equally spaced illumination functions across the main array, one corresponding to each beam of the multiple beam feed. Assuming an even number of subarray input ports to the feed matrix, the geometry is selected so that after proper adjustments for collimation each beam (p) of the feed radiates to produce an illumination  $g(\eta - q)$  at the input to the phase shifters at the radiating face of the circular lens, where

 $\eta = x/D$ 

Borgiotti, G.V. (1977) An antenna for limited scan in one plane: design criteria and numerical simulation, IEEE Trans. AP-25:232-243.

$$q = p - 1/2$$

and D is the distance between each subarray center measured at the front lens face.

The phase shifters at the front of the lens are set to form a progressive phase tilt that is a discrete sampling of the continuous function:

$$-2\pi\left(\frac{x}{\lambda_o}\sin\theta_o\right)$$
.

The radiation pattern corresponding to each of the phase-shifted subarray illuminations is called the subarray pattern and is given by the following expression (after removing the relative phase displacement  $2\pi q D/\lambda_0 \sin \theta_0$  at the p-th subarray):

$$f(p) = \frac{1}{K} \int_{-I/2}^{I/2} e^{j2\pi(\eta - q)\beta_a} g(\eta - q) d\eta$$
 (1)

for

$$\beta_{a} = RS - S_{o} ,$$

$$I = L/D ,$$

$$S = (D/\lambda_{o}) \sin \theta ,$$

$$S_{o} = (D/\lambda_{o}) \sin \theta_{o} ,$$

$$R = \lambda_{o}/\lambda$$

and

K = normalizing factor.

Adding time-delay elements at the input of each subarray port to provide time delay corresponding to the distance Dq sin  $\theta_{\rm C}$  for collimation at some angle  $\theta_{\rm C}$  (which may or may not correspond to the angle of the center frequency subarray beam center  $\theta_{\rm O}$ ) results in radiation characteristics for the complete array, as given by:

$$F(S) = \sum_{p=\frac{-N}{2}+1}^{\frac{N}{2}} I_{p} f(p) e^{j2\pi qR(S-S_{c})}.$$
 (2)

The array pattern is the weighted sum of the subarray patterns. If the spacing D is more than half a wavelength, the resulting pattern will have grating lobes at angles  $\theta$  given by:

$$\sin \theta = \sin \theta_{c} + n \frac{\lambda}{D} \quad . \tag{3}$$

In the limiting case when all subarray patterns are the same, the array radiation pattern is the product of the subarray pattern and the array factor, so the grating lobe amplitude increases with the subarray sidelobe.

Thus the tapered distribution Ip controls the level of the near sidelobes (within the subarray pattern), and the subarray sidelobes control the level of the far sidelobes, because these are the grating lobes of the array factor.

The array pattern F(s) is time-delay scanned and does not squint (the peak is always at  $sin \theta = sin \theta_c$ ), but the subarray pattern is a function of (RS -  $S_0$ ) and squints with frequency, as indicated schematically in Figure 1. For this reason, the previous developments,  $^1$  have emphasized the formation of pulse-shaped subarray patterns to provide grating lobe suppression over a given band of frequencies. Such patterns are formed by an orthogonal hybrid network or lens with equal amplitude output coefficients. A signal applied to one of the input ports excites a set of uniformally illuminated output signals corresponding to one of the multiple beams.

The feed array excites the main array with an illumination given approximately by

$$g(n-q) = \sin \pi (n-q)/\pi (n-q)$$
 (4)

If l were infinite, this excitation would produce a flat-topped pattern l(p) constant for  $|\beta_a| = |RS - S_0| < 1/2$  and zero for  $\beta_a$  outside of that region, as shown schematically in Figure 1. This pattern provides perfect grating-lobe suppression for a very large array over a frequency bandwidth of approximately  $l/S_0$ . Unfortunately, the truncation of this illumination function causes relatively high subarray sidelobes and, hence, can result in unacceptable grating lobe levels for certain array sizes and illumination parameters Ip.

Figure 2 shows several subarray and array patterns for an array 10 subarrays wide (t=10) with the central 8 subarrays active. Since the subarray pattern is a function of the angular difference parameter  $\beta_a = D/\lambda \sin \theta - D/\lambda_0 \sin \theta_0$  and not a function of the scan angle  $\sin \theta_0$  alone, all figures shown in this report are plotted with  $\theta_0$  equal to zero, but apply equally well to scanned or unscanned subarray patterns with the  $\cos \theta$  projection factor introduced appropriately. A more thorough analysis would include lens element patterns and mutual coupling effects, but that analysis is beyond the scope of this report.

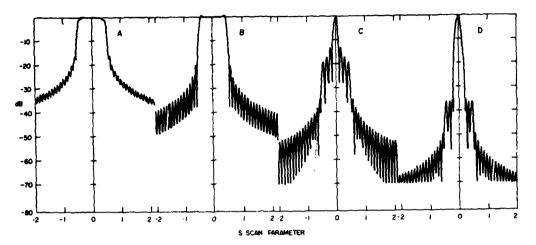


Figure 2. Subarray Feed With no Output Taper: A. Edge Subarray Pattern (p = -3), B. Central Subarray Pattern (p = -1), C. Radiation Pattern for Uniformally Illuminated Array, D. Radiation Pattern for Array With -35 dB Chebyshev Taper

A comparison of the subarray patterns for p = -3 and p = -1 demonstrates the deleterious effect of truncation near the array edge, and suggests the possibility of array pattern deterioration. Figure 2C shows the array radiation pattern when the subarrays are excited uniformly  $\{Ip\}=1$  and indicates significant suppression outside of the subarray angular passband, but it also shows the radiation in the grating lobe regions to be much larger than -50 dB, and so not compatible with truly low sidelobe performance. Figure 2D shows that for a -35 dB Chebyshev taper the effects of edge truncation are minimal and distortion of the subarray pattern does not lead to significant radiation in the grating lobe region. One other characteristic of these subarray patterns is worthy of notice, however, and that is that the ripples within the subarray passband are very different for the various subarrays; this suggests difficulty in forming wideband nulls at the array level, because the null formed at one frequency would not be null at another frequency since the subarray patterns do not all vary together.

As an example of an alternate approach, the curves shown in Figure 3 correspond to a feed taper given by the function  $c + \cos^2(\pi y/2b)$  for c = 0.071. This is indeed a severe example of feed amplitude taper, and it is used here for illustrative purposes only. The subarray illumination for this familiar function has the form:

$$g(\eta - q) = \frac{\sin \pi (\eta - q)}{\pi (\eta - q)} \left[ c + \frac{1}{2} \frac{1}{(1 - (\eta - q)^2)} \right] . \tag{5}$$

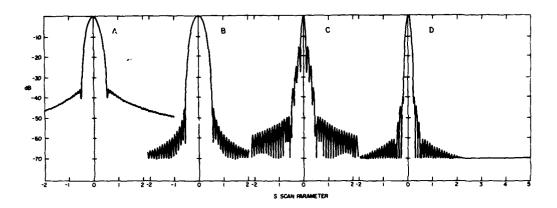


Figure 3. Subarray Feed With Tapered Output: A. Edge Subarray Pattern (p = -3), B. Central Subarray Pattern (p = -1), C. Radiation Pattern for Uniformally illuminated Array, D. Radiation Pattern for Array With -35 dB Chebyshev Taper

This illumination has such low sidelobes that its radiation pattern is essentially unaltered by truncation and has the same form as the feed taper (in the angular coordinate "S") because both the feed network illumination and the radiation pattern are obtained by taking the Fourier transform of the subarray illumination. Figure 3 shows this subarray pattern to have extremely low sidelobes but inferior bandpass characteristics as compared with orthogonal subarrays. In addition, the non-orthogonal nature of the feed distribution will introduce significant losses in the multiple beam network; therefore, system efficiency may dictate the use of linear amplifiers at the subarray feed. However, the use of this distribution illustrates the possibility of producing excellent grating lobe control with low sidelobe subarray patterns even for truncated subarray illuminations, as indicated by comparing Figures 3A and B. Figures 3C and D show that one can obtain excellent grating lobe control with an eight-element array of these subarrays with uniform or -35 dB Chebychev illumination. Moreover, within the angular passband, the subarray radiation patterns are so similar across the array that wideband null steering is possible at the array level by using algorithms for null steering at the array terminals (subarray ports).

In addition to array level null steering, control of the feed taper provides a mechanism for creating nulls in the subarray pattern. At first glance it would seem that simply forcing the feed array excitation to be zero over an extended part of the feed would produce a subarray pattern with a wide nulled area. Figure 4 shows the subarray pattern that results from the use of a feed illumination given by:

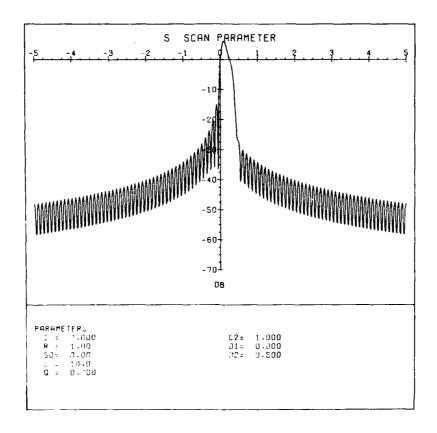


Figure 4. Subarray Pattern for the Truncated Distribution of Eq. (12)

$$a(y) = c + cos^2 \frac{\pi y}{2b}$$
 for  $-b < y < 0$   
= 0 for  $0 < y < b$ .

Such an illumination is suggested by the existing dual transform relationship which states that in the absence of truncation, the subarray pattern and subarray feed illumination are the same; therefore, one would expect at first that the subarray pattern of Figure 5 would have a wide trough as appropriate for wide band null formation within the subarray. Unfortunately, Figure 4 shows that this distribution suffers so severely from the effects of truncation that the trough area is filled with sidelobes.

A more successful technique for forming wide band subarray nulls follows from the use of one or several tapered illuminations instead of the discontinuous illumination above. One such feed illumination is:

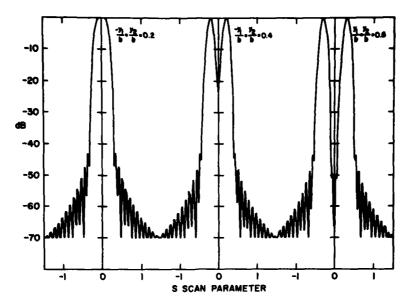


Figure 5. Subarray Patterns for the Illumination of Eq. (14)

$$a(y) = \left[c + \cos^{2}\left(\frac{\pi(y - y_{1})}{2\Delta_{1}}\right)\right] y_{1} - \Delta_{1} < y < y_{1} + \Delta_{1}$$

$$= \left[c + \cos^{2}\left(\frac{\pi(y - y_{2})}{2\Delta_{2}}\right)\right] y_{2} - \Delta_{2} < y < y_{2} + \Delta_{2} ,$$
(7)

and the resulting subarray illumination has the form

$$g(\eta - q) = \frac{\Delta_{1}}{b} e^{j\pi y} 1^{(\eta - q)} \left( \frac{\sin \pi [(\eta - q) \Delta_{1}^{'}b]}{\pi \frac{\Delta_{1}}{b} (\eta - q)} \right) \left( c + \frac{1}{2} \frac{1}{\left( 1 - \left( \frac{\Delta_{1}}{b} \right)^{2} (\eta - q)^{2} \right)} \right) + \frac{\Delta_{2}}{b} e^{j\pi y} 2^{(\eta - q)} \left( \frac{\sin \pi [(\eta - q) \Delta_{2}^{'}b]}{\pi \frac{\Delta_{2}}{b} (\eta - q)} \right) \left( c + \frac{1}{2} \frac{1}{\left( 1 - \left( \frac{\Delta_{2}}{b} \right)^{2} (\eta - q)^{2} \right)} \right).$$
(8)

Figure 5 shows the subarray patterns for this illumination with

$$\left(\frac{\Delta_1}{b}\right) = \left(\frac{\Delta_2}{b}\right) = 0.4 \quad ; \quad c = 0.071$$

$$I = 10$$

and

$$\frac{-y_1}{b} = \frac{y_2}{b} = 0.2$$
 , 0.4 and 0.6.

These curves show the resulting subarray pattern can be varied from a nearly flat-topped pattern to one with a wide trough between two peaks. The data for  $-y_1 = y_2 = 0.2b$  suggests immediately that far greater bandwidth can be obtained from a flat-topped illumination with tapered edges than was achieved with the  $\cos^2$  on a pedestal distribution used previously, and one might seek further optimization along these lines. As the spacing between the two illumination functions is increased to  $-y_1/b = y_2/b = 0.4$  and 0.6, a null is formed over a frequency range that is proportional to the width of the trough, so the ability to control such a deep, broad trough aids substantially in wide band null control. Since  $\theta_c \neq \theta_0$ , it is possible to keep the subarray null fixed in position while scanning the beam over a limited sector. Alternatively, full scan capability is maintained by scanning the main beam and the subarray null.

Perhaps the most useful means of interference suppression with such a system would simply be to narrow the subarray pattern, using a tapered illumination like one of the functions in Eq. (8), or some other distribution that uses only a part of the feed array, then to use the steep skirts of the subarray pattern to discriminate against the unwanted noise signal.

In order to present a design technique for controlling the subarray pattern width in the presence of an undesired signal, it is convenient first to define the parameters determining the subarray pattern.

The main lens aperture illumination function is given by the far field expression

$$g(x) = \int_{-\infty}^{\infty} f(y) \cdot e^{jk_0 y \sin \phi dy} = \int_{-\infty}^{\infty} f(y) e^{jk_0 y(x/a)dy}$$
(9)

for a lens of radius a and a feed excitation f(y) defined with the region

$$-b_1 \le y \le b_2 \quad , \tag{10}$$

which is smaller than the full extent of the feed (Figure 2B).

The subarray far field pattern, as indicated in Eq. (1), is related to the Fourier transform of this truncated aperture illumination modified by the imposed phase shift. This dual transform relationship implies that the far field pattern of the scanned subarray is, apart from truncation effects, the same expression as the feed illumination f(y) with the parameter y replaced by the angle variable:
-a  $(\sin \theta - \lambda/\lambda_0 \sin \theta_0)$ . The subarray pattern is therefore defined within the region

$$\frac{-b_2}{a} \le \left(\sin\theta - \frac{\lambda}{\lambda_0}\sin\theta_0\right) \le \frac{b_1}{a} \tag{11}$$

and is essentially zero outside of that region.

The above condition results from geometric considerations of the feed. The suppression of grating lobes imposes a constraint on the size (Figure 2B) of the feed array, for, in order to obtain grating lobe suppression at a given wavelength  $\lambda$  for a beam at  $\theta_{\rm C}$  =  $\theta_{\rm O}$ , the width of the subarray pattern is constrained by the condition

$$-\frac{1}{2} \le \frac{D}{\lambda} \cdot (\sin \theta - \sin \theta_0) \le \frac{1}{2}$$
 (12)

for inter-subarray distance D.

Using this expression and the previous one leads to the condition defining the subarray feed size at the highest frequency, assuming that the subarray width is chosen to allow scan to some maximum angle  $\theta_{\rm max}$  with S<sub>O</sub> equal to zero. This results in the conditions

$$\frac{b}{a} \left( \frac{D}{\lambda \min} \right) = \frac{1}{2} \quad \text{and} \quad S_{\max} \le \frac{1}{2} \frac{\lambda_{\min}}{\lambda_{o}}$$
 (13)

and to the final expression for the subarray width as a function of the excited fraction of the aperture:

$$-\left(\frac{\lambda_{\min}}{\lambda}\right)^{\frac{b_2}{2b}} \leq \frac{D}{\lambda} \cdot \sin \theta - \frac{D}{\lambda_0} \sin \theta_0 \leq \frac{b_1}{2b} \left(\frac{\lambda_{\min}}{\lambda}\right). \tag{14}$$

Equation (14) can be used to derive handwidth constraints and to determine the optimum illuminated region of the subarray face in the presence of unwanted noise signals. For example, as indicated in Figure 6A, if an interferring signal radiates at an angle  $\theta_j$  (in this case we assume  $\theta_j > \theta_0$ ) and operates over a frequency range bounded by the lower frequency with wavelength  $\lambda_j$  max and upper frequency with  $\lambda_j$  min, then the system upper frequency (with wavelength  $\lambda$  min) is bounded by the condition

$$\frac{D}{\lambda_{\min}} \sin \theta_{0} \le \frac{D}{\lambda_{j} \max} \sin \theta_{j} , \qquad (15)$$

which serves to define the parameter b, using Eq. (14):

$$\frac{D}{\lambda_{j} \max} \sin \theta_{j} - \frac{D}{\lambda_{o}} \sin \theta_{o} = \frac{b_{1}}{2b} \left( \frac{\lambda \min}{\lambda_{j} \max} \right) . \tag{16}$$

This restriction ( $b_1 < b$ ) causes the subarray pattern to be narrowed so as to eliminate the signal at the angle of the interference in accordance with Eq. (15). Since this example places no constraint on the lower frequency limit, the dimension  $b_2$  can be made equal to b.

Use of Eq. (14) at the system upper and lower frequencies leads to the following expression for system bandwidth as measured to the pattern nulls (again for a main beam at  $\sin \theta$ ):

$$BW = \frac{f \max - f \min}{f_o} = \left(\frac{b_1}{2bS_o} + 1\right) \left[1 - \frac{S_o}{S_o\left(\frac{b_1}{2bS_o} + 1\right) + \frac{b_2}{2b}}\right] . \quad (17)$$

Although this analysis has been carried out assuming generalized feed illuminations, the use of uniform illumination within the feed region  $-b_2 \le y \le b_1$  will result in unduly large truncation sidelobes, as shown in Figure 4, and the illumination throughout this region must be tapered to minimize null filling due to truncation. Figure 6b shows the narrowed subarray illumination corresponding to Eq. (8) with the parameters

$$\left(\frac{\Delta_1}{b}\right) = \left(\frac{\Delta_2}{b}\right) = 0.4$$
,  $\frac{y_1}{b} = +0.2$ ,  $\frac{y_2}{b} = +0.6$ ,  $l = 10$  and  $c = 0.071$ ,

and so gives one example of a narrowed subarray pattern with low sidelobes.

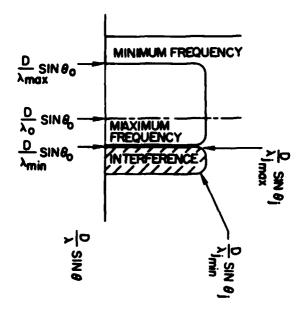


Figure 6A. Narrowed Subarray for Interference Rejection

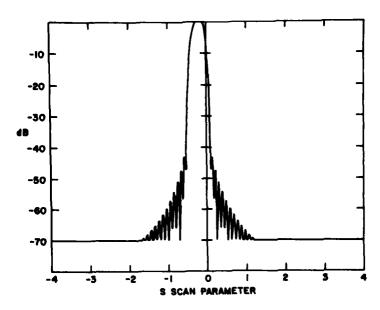


Figure 6B. Narrowed Subarray Pattern Using Eq. (8)

Since Eq. (17) gives bandwidth as measured to the null frequency, the actual bandwidth is less because of pattern falloff, and the use of a severely tapered illumination such as the  $\cos^2\theta$  functions used for illustrative purposes throughout this report tends to further restrict bandwidth.

Such subarray pattern control, as required to narrow the subarray pattern and avoid interfering signals, can be implemented either adaptively or deterministically. The deterministic solution can be obtained from the above equations directly, based upon knowledge of the position and bandwidth of the interfering and desired signals. The adaptive solution would differ in principle from conventional algorithms in that the adaptive weighting is applied at the subarray feed aperture and that it should discriminate on the basis of received frequency and location of the received signal on the feed aperture. Since the received signal from any one point in space is projected to different areas on the feed surface, depending upon the source frequency, then by discriminating on the basis of frequency and feed illumination the technique can accommodate null placement in the direction of any interfering source, unless it occupies the same frequency spectrum limits and angular location as the desired source.

#### 3. CONCLUSION

This analysis has treated the case of an optically subarraying feed with amplitude control at the feed aperture. The two main conclusions are that the feed taper can result in extremely low sidelobe subarray patterns and can produce subarray troughs consistent with wideband null formation.

The increased loss resulting from use of such non-orthogonal subarray illuminations is best compensated using amplifiers at the feed aperture, but with this loss overcome the system allows a degree of control not available with other types of subarraying systems. This added control includes the ability to form low sidelobe subarray patterns for wide band performance, the formation of subarray nulls or troughs with reasonable bandwidth and good array sidelobes, and combinations of the above.